



## Urban Rainwater Management and Protection Through Optimization for Multiple Goals

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**ABSTRACT:** *With the continuous acceleration of urbanization, urban rainwater management has become an increasingly important issue. In the process of urbanization, the increase in impervious area and insufficient drainage systems have led to an increase in rainwater runoff and a risk of water quality deterioration. This article explores the application of multi-objective optimization in landscape urban rainwater design and defense. Against the backdrop of accelerating urbanization, rainwater management has become an important issue. By introducing multi-objective optimization methods, the aim is to seek a more comprehensive and effective rainwater design solution to address the impact of urbanization on rainwater.*

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### 1. Introduction

*In recent years, the rainstorm disasters in our country are more and more frequent. According to the analysis, there are several reasons for this situation. The first is that the high-speed urbanization process has resulted in the hardening of a large amount of high-permeability natural ground and increased the initial runoff of the ground [1]. Second, the construction of drainage facilities cannot keep up with the pace of urban development and take more single-purpose engineering measures in urban storm water systems. The lack of consideration of the integrity of aquatic ecosystems has resulted in the damage or even complete destruction of the ecological service functions of the natural ecosystems associated with rainwater Loss of function [2]. It is an irresistible factor that global warming in recent years, rising sea levels and the frequent occurrence of extreme weather has led to the destructive power of natural disasters. Rainfall has far exceeded the capacity of urban drainage and drainage facilities [3]. Water is the source of life, the blood of industry, the lifeblood of cities and the rational management of water resources are the preconditions for the sustainable development of urban health. How to make disasters into available water resources is an important part of water resources utilization management in the new*

situation [4]. In view of the actual situation of urban rain-storm in our country, how to use rainwater and floods for humanity scientifically is an important research topic before the whole society. Among them, city construction of cotton city is a combination of open source and festival the decision of important functions of flow can effectively alleviate or even solve the problem of rain that distress people. However, it is still in the process of implementation for various reasons [5].

## 2. State of the Art

Multi-objective Optimization Problems (MOPs) originated in the design, modeling and planning of many practical complex systems in areas such as industrial manufacturing, urban transport, capital budgeting, forest management, reservoir management, new City layout and landscaping, energy distribution, etc. [6]. In almost every important real-life decision-making problem, there are a number of conflicting goals that must be considered while considering different constraints. These issues all involve the optimization of multiple goals that do not exist independently. They are often the culprit Together for competing goals, each goal has a different physical meaning and dimension [7]. Their competitiveness and complexity make it difficult to optimize them. Multi-objective optimization is a new discipline in applied mathematics that has developed rapidly in recent 20 years. It investigates the optimization problem in some sense when the vector objective function satisfies certain constraints. Since a large number of real-world problems can be summed up as optimization problems with multiple objectives, the research on multi-objective optimization has attracted great attention both nationally and internationally since the 1970s [8]. Especially in the past 10 years or so, theoretical exploration has been deepened, the scope of application has been increasingly widened, the research team has grown rapidly and shows great vitality. At the same time, as the research on large and complex systems in socioeconomic and engineering design progresses, the theories and methods of multi-objective optimization are continually challenged and rapidly developed [9].

## 3. Methodology

### 3.1 Multi-objective Optimization Of The Mathematical Model

**Decision variables:** Both water level and discharge volume need to be controlled, so the decision variables in the operation rules can be broadly divided into two categories. **Category 1:** Controlled water levels at the outlet section of the control section. From the water level ZC, flood control flood level or daily water level lower limit, the corresponding storage for the VC. Return water level ZS, daily water level cap, the corresponding storage capacity for the VS. The highest flood storage ZM is, the corresponding storage for the VM. **Class 2:** Control sluice outlet sluice characteristics. Maximum discharge; emergence time; peak recovery time TS. Type 2 operating rules are determined by the statistical model. Under a set of

ZC ZS ZM conditions, the floods of historical hydrological data are adjusted and calculated, and then, according to the inflow and discharge eigenvalue of each flood, through regression Analyze and establish statistical models [10].

**The objective function. Optimization guideline 1:** Flood loss (expressed as disaster-prone water volume) Min

$$f_1 = \min \sum_{n=1}^N DW_n \quad (1)$$

**Optimization Criterion 2:** Xingyi Benefit (expressed as effective water storage in the river channel) is the largest

$$f_2 = \max \sum_{n=1}^N \sum_{t=1}^T [(Q_{t,n} - D_{t,n}) \Delta t] \quad (2)$$

Where  $n$  is the rain flood sequence number,  $n = 1, \dots, N$ ;  $\Delta t$  for the time step, s;  $DW_n$  for the nth flood disaster water,  $m^3$ ;  $Q_{t,n}$   $D_{t,n}$  respectively for the nth flood  $t$  inflow and discharge flow period.  $m^3/S$  Constraints as shown below,

$$\begin{cases} ZC < ZS < ZM \leq Z_m \\ ZC_l \leq ZC \leq ZC_m \\ ZS_l \leq ZS \leq ZS_m \\ ZM_l \leq ZM \leq ZM_m \end{cases} \quad (3)$$

Where to allow the highest flood level; with the subscript "m" for the lower limit of the water level; with subscript "m" for the upper limit of the water level.  $DW_n$  and  $D_{t,n}$  of the objective function are non-linear functions of the decision variables. Moreover, the two sub-targets are mutually contradictory. For example, ZC is low, which is good for flood control and DW is small. However, in the case of small floods, the probability of losing to ZS will decrease and  $f_2$  will decrease. So the model is more Variables, multi-objective nonlinear rules (NLP) problems.

### 3.2. Multi-objective Optimization Algorithm Basic Principles

The essence of MOP is that in most cases, all sub-goals may be in conflict with each other. The improvement of some sub-goals may result in the reduction of the functions of the other sub-goals. At the same time, it is unrealistic to promote many sub-goals at the same time and vice versa In the range of multi-objective optimization analysis. The final solution to MOP can only be to make a full measure of trade-off between each sub-goal and to make each sub-objective function as optimal as possible. Therefore, there exists a certain difference between the optimal solution of MOP and the optimal solution of single-objective optimization problem. In order to solve MOP effectively, the definition of solution should be summarized.

**Definition 1.2 (feasible solution set):** A feasible solu-

tion set  $X_f$  represents a set of decision vectors  $x$  that satisfy the constraint  $e(x)$  in formula (2-1), that is,

$$X_f = \{x \in X \mid e(x) \leq 0\} \quad (4)$$

$X_f$  feasible range associated with the target space formula is as follows:

$$Y_f = f(X_f) = Y_{x \in X_f} \{f(x)\} \quad (5)$$

For Eq. (2-3), we denote all  $x$  in the feasible solution set  $X_f$ , and realize a subspace in the target space through the optimization function mapping. The relevant decision vectors in that subspace belong to the feasible solution set.

One of the subspaces, the relevant decision-making vector of that subspace belong to the feasible solution set.

For the minimization problem, it can be directly converted into the above maximization problem to be solved.

The feasible solution set of single-objective optimization problem can be based on its designated objective function  $f$  to determine the relationship between the advantages and disadvantages of the method. For the MOP problem, the situation is different, because in general, the decision-making vector of  $X_f$  cannot be completely sorted, and only some of the indicators can be sorted, that is, local sorting.

The multi-objective optimization algorithm mainly sorts  $k$  objective functions of the MOP problem by their importance. For example, it may be assumed that the  $k$  objective functions of the MOP problem have been sorted:  $f_1(x)$  the most critical,  $f_2(x)$  times,  $f_3(x)$  again, ..., and the last one represents  $f_k(x)$ . First find the relevant issues:

$$\begin{cases} \text{Maximize } f_1(x) \\ \text{S.t. } e(x) = (e_1(x), e_2(x), \dots, e_m(x)) \leq 0 \end{cases} \quad (6)$$

Optimal solution to the problem  $x(1)$  and optimal value  $f_1^*$ . which is:

$$f_1^* = \text{Max}_{x \in R_1} f_1(x) \quad (7)$$

Among them,  $R_1 = X_f$  and to solve the problem:

$$\begin{cases} \text{Maximize } f_2(x) \\ \text{S.t. } x \in R_2 \end{cases} \quad (8)$$

Optimal solution to the problem  $x(2)$  and optimal value  $f_2^*$ . which is:

$$f_2^* = \text{Max}_{x \in R_2} f_2(x) \quad (9)$$

And  $R_2 = R_1 \cap \{x \mid f_1(x) \geq f_1^*\}$ , continue to solve the problem:

$$\begin{cases} \text{Maximize } f_3(x) \\ \text{S.t. } x \in R_3 \end{cases} \quad (10)$$

Optimal solution to the problem  $x(3)$  and optimal value  $f_3^*$ . which is:

$$f_3^* = \text{Max}_{x \in R_3} f_3(x) \quad (11)$$

And  $R_3 = R_2 \cap \{x \mid f_2(x) \geq f_2^*\}$ . So go on until you find the  $k$ th question:

$$\begin{cases} \text{Maximize } f_k(x) \\ \text{S.t. } x \in R_k \end{cases} \quad (12)$$

Optimal solution to the problem  $x(k)$  and optimal value  $f_k^*$ . which is:

$$f_k^* = \text{Max}_{x \in R_k} f_k(x) \quad (13)$$

And  $R_k = R_{k-1} \cap \{x \mid f_{k-1}(x) \geq f_{k-1}^*\}$ , the resulting  $x(k)$  is the optimal solution of the MOP problem in the sense of hierarchical sequence, that is,  $x^* = x(k)$ .

$$F^* = (f_1(x^*), f_2(x^*), \dots, f_k(x^*)) \quad (14)$$

$F^*$  represents the optimal value of the MOP problem. In most cases, the optimal solution that is close to the single-objective optimization is not among the multiple objective optimization problems, only the Pareto optimal solution exists. The Pareto optimal solution of multiple objective optimization problems is only one of its satisfying or non-inferior solutions that can be adopted, while the general multi-objective optimization problems often have multiple Pareto optimal solutions. If a multi-objective optimization problem has a so-called optimal solution, then the optimal solution must be the Pareto optimal solution, while the Pareto optimal solution is composed of only those optimal solutions and does not include other solutions. So Pareto optimal solution is usually a valid solution to multiple objective optimization problems. The general Pareto optimal solutions to multiple objective optimization problems belong to a category of ensembles. For the practical application problem, one or more of the Pareto optimal solutions of the multiple objective optimization problems need to be considered as the optimal solution of the multiple objective optimization problems to be solved by grasping the degree of the problem and the preference of the decision maker. Therefore, the solution to multiple objective optimization problems and the key is to find as many Pareto optimal solution.

### 3.3 Multi-objective Optimization Solution

Because the non-linear function between the objective function and the decision variable is difficult to express

analytically, it can only get the corresponding target value by adjusting the calculation under the control of the first category of operation rules. Therefore, the direct search method is used to seek the optimal solution. The author proposes to combine grid search with subsection control lumped water division adjustment calculation method to solve the above model and get two sub-objective values under various decision vectors  $X=(ZC \ ZS \ ZM)t$ , and then make multi-objective decision to obtain satisfactory solution.

**Grid search method:** the ZC ZS ZM in the feasible domain by a certain amount of discrete elements to form a grid. Only for the entire network-related decision-making vector to be adjusted to calculate, through a certain calculation to obtain the target value of  $f_1, f_2$ ; and then select the satisfactory solution through the multi-objective decision-making program, that is, the first class of operation requirements of the three control water level(ZC ZS ZM).

**Segmented control lumped water partitioning method:** This method is used to give all the control of water level and allow the maximum flood water flow requirements under the river flood adjustment calculation. Under the control of the exit gate of the river, the upper reach of the gate can be regarded as a storage area with the capability of detention. In view of the characteristics of river-type detention basin, the author proposes the subsection control lumped water division method to simulate the flood regulation. The so-called sub-control refers to the urban area is divided into North protection, South care and Dongzhimen, Longtan gate to Lejia Garden three major rivers; lumped refers to the three major sections of the rainfall runoff, respectively, to focus on the most downstream of the river control Section of the inflow process said; water cut refers to the runoff is divided into sluggish, venting, flood diversion, disaster several parts, through the water cut to determine the release process.

The basic principle of segmentation is water balance. The total amount of water in a flood control section is divided into WS water storage capacity WS, the amount of discharge DC, outward flood diversion DF and in case of heavy rain due to lack of flood control capacity caused by the amount of water DW.

$$W = WS + DC + DF + DW \quad (15)$$

According to the total amount of floods and system operation characteristics of W classification control:

Firstly,  $w \leq S_s$  ( $S_s = VS - VC$ ), W fully stored in the river:

$$W = WS \quad (16)$$

Secondly,  $S_s \leq W \leq S_m$  ( $S_m = VM - VC$ ), The flood water first stored in the river, part of the water after the peak discharge DS, the water level back to the ZS, as shown in Figure 1.

$$W = WS + DC - DS \quad (17)$$

Thirdly,  $w \geq S_m$ , according to the flood control conditions of the outflow basin, the following three conditions:

$$\begin{cases} Q_m \leq QK, W = S_m + DC - DS \text{ Not flood} \\ Q_m > QK, W = S_m + DC + DF - DS \text{ flood} \\ Q_m > QK + QF_m, W = S_m + DC + DF + DW - DS \text{ flood} \end{cases} \quad (18)$$

In the formula,  $Q_m$  is the peak flow;  $QK$  is the flood diversion critical flow;  $QF_m$  is the outward flow basin maximum flood flow. If the water return duration is less than two consecutive rainfall intervals, then adjust the single peak, as shown in Figure 1,2; otherwise, according to the bimodal adjustment, shown in Figure 3

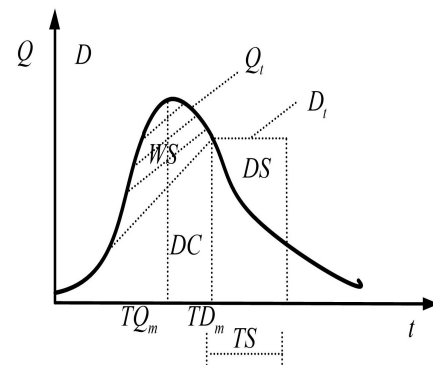


Figure 1. Unimodal regulation a

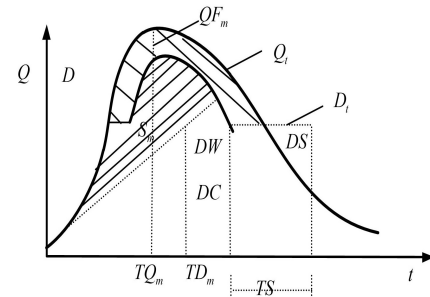


Figure 2. Unimodal regulation b

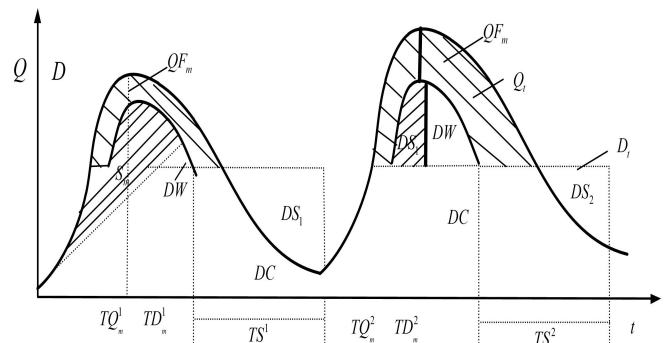


Figure 3. Shuangfeng regulation

Drainage form of choice: In order to consider the benefits of flood control and prosperous, flood gates continue to open to achieve the maximum discharge of after , until the water level back to sluice sluice back to the ZS, will reduce the opening, the control discharge ~ To flow, so the actual discharge part was ladder-shaped. In the analysis of operational rules, the flood section of the discharge section is simplified to a straight line, see the dotted line in Figure 1,2,3.

The core steps of the preferred operation rules are: First, the decision vector  $X=(ZC\ ZS\ ZM)t$  is assigned to the first type of operation rules by the grid search method. Secondly, according to given ZC ZS ZM and , the total sub-target values related to the entire decision vector are calculated and adjusted for each flood in the historical hydrological information by the lumped water cut method.

Thirdly, a satisfactory solution is sought by using the multi-objective gray situation decision-making method, that is, the preferred Class 1 operating rules  $X^*=(ZC\ ZS\ ZM)^*.s$

Fourth, with the selected long series of (ZC ZS ZM)\* corresponding to adjust the calculation results, regression analysis, the establishment of , , TS statistical scheduling model.

#### 4. Result Analysis And Discussion

##### 4.1 . Experimental Results And Analysis

Applying the above models and solving methods, taking the collected data of the maximum rainfall of 1 ~ 2 times in 1977 ~ 1992 years and the data of 1959 and 1963 heavy rainfalls as the model input, a long series of calculations were made and a satisfactory multi-objective Conversion algorithm operation rules. Grid of the first type of operation rules ZC, ZS and ZM of the two control sections of Dongzhimen and Longtan gates are discretized by their respective increments in their feasible domains to form a grid. The discrete values are shown in Table 1. Each dot corresponds to a decision vector X.

Table 1. Combination Schemes for Operation Rules of the First Type

Control section name	ZC(m)	ZS(m)	ZM(m)	$QK(m^3/s)$	$QF_m(m^3/s)$	Number of constituent dots
Dongzhime n sluice	38.5	39.5	40.5	60	30	9
	38.6	39.6				
	38.7	39.7				
Longtan sluice gate	35.7	36.7	37.5	120	40	6
	35.8	36.8				
	35.9					

Table 1. Combination Schemes for Operation Rules of the First Type

Corresponding adjustment capacity of each network point: For Songlin Gate ~ Dongzhimen Gate of North Guard and You'an Dam ~ Longtan Sluice of South Protection, the surface waterlines corresponding to ZC, ZS and ZM

ZC(m)	ZS(m)	ZM(m)
38.5	39.5	40.5
	39.6	
	39.7	
38.6	39.5	40.5
	39.6	
	39.7	

Table 2. Storages Responding to Characteristic Water Levels of Dongzhimen Sluice

Goal decision-making - the first type of operation rules is preferred, which is the event of the optimized scheduling of north protection and south-guard rain-flood system re

are respectively calculated by the non-uniform flow channels of open channel, According to the river section data, the inventory of XingLi and flood control capacity are obtained, see Table 2 and Table 3.

ZC(m)	ZS(m)	ZM(m)	$S_m(10^4m^3)$
35.7	36.7	37.5	61.5
	36.8		59.6
35.8	36.7		

Table 3. Storages Responding to Characteristic Water Levels of Longtan Sluice

spectively. The first category of operation rules is the countermeasure, and the two constitute the situation. Each situation has a corresponding sub-goal f1 and f2, consti-

tute the effect of the whitening value matrix, the use of multi-objective gray situation decision-making method, the choice of a satisfactory type 1 operating rules:

North rain rains system:(ZC ZS ZM)\*=(38.5 39.7 40.5)  
South rain rains system:(ZC ZS ZM)\*=(35.7 36.7 37.5)

The second type of statistical operation model of the scheduling model to corresponding to the long series of flood regulation calculation results for the sample, statistics, the main discharge characteristic value of  $D_m$ ,  $TD_m$ , TS and incoming water characteristic value of  $Q_m$ : peak flow and its occurrence time of  $TQ_m$ , Secondary rainfall P, rainfall intensity i, secondary net depth R and so on. Then, the regression relationship between the discharge characteristic value and the incoming water eigenvalue is analyzed to establish a statistical scheduling model. North East Protection Gate is now an example as follows:

First, the maximum discharge  $D_m$  is related to the characteristic value of incoming water. Several regression relationships of  $D_m \sim P$ ,  $D_m \sim i$ ,  $D_m \sim R$  and  $D_m \sim Q_m$  have

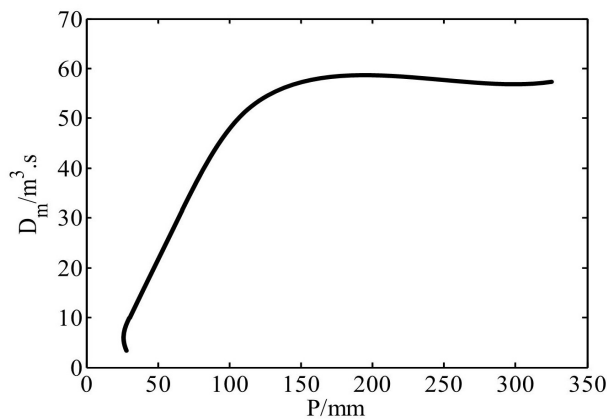
been tested. The correlation between  $D_m \sim P$  is the most significant and P can be measured directly Got it. Second, the occurrence of , and water come from the eigenvalue test  $TD_m \sim Q_m$ ,  $TD_m \sim TQ_m$ ,  $TD_m \sim P$  several relations, with  $TD_m \sim TQ_m$  correlation is very significant. Thirdly, the relation between TS TS and water inflow eigenvalue was tested in the relationship of  $TS \sim P$ ,  $TS \sim Q_m$  and  $TS \sim D_m$ , and the most significant correlation was  $TS \sim D_m$ . The regression analysis, the establishment of Dongzhimen gate type 2 operating rules of the statistical model is:

$$D_m = \begin{cases} -0.0028P^2 + 0.9216P - 16.5237 & 20 \leq P \leq 166.5 \text{ mm} \\ 60 & P \geq 166.5 \text{ mm} \end{cases} \quad (19)$$

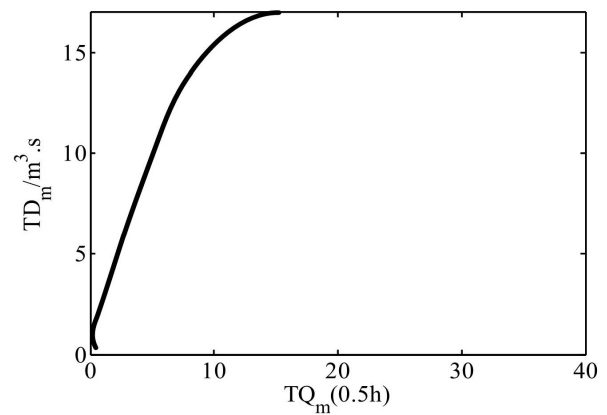
$$TD_m = -0.0631TQ_m^2 + 2.1992TQ_m - 2.2707 \quad (20)$$

$$TS = 1/(-0.00016D_m^2 + 0.0176D_m - 0.0445) \quad (21)$$

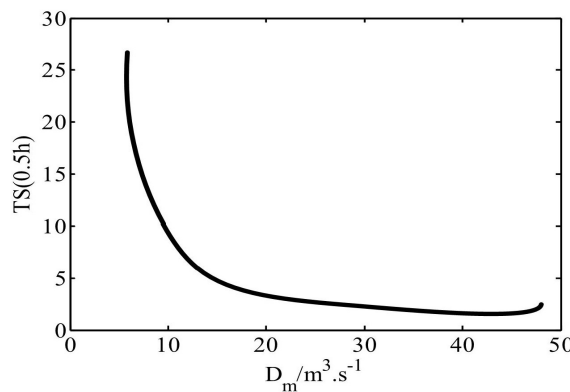
Figure 4 (a), (b), (c) gives  $D_m \sim P$ ,  $TD_m \sim TQ_m$ ,  $TS \sim D_m$  correlation diagram.



(a)  $D_m \sim P$



(b)  $TD_m \sim TQ_m$



(c)  $TS \sim D_m$

Figure 4. Correlatographs between  $D_m$  and P,  $TD_m$  and  $TQ_m$ , and TS and  $D_m$  at Dongzhimen sluice

The first type of operating rules are mainly used for long-term flood season operation, not with the year and rainfall changes in size. No matter how much flood you encounter the water, Dongzhimen gate and Longtan gate all control the storage, drainage, flood diversion and storage of the flood tail according to the preferred Class 1 operation rules (ZC ZS ZM). The second type of operation rules are mainly used for the second flood regulation, hydrological forecasting needs to be used. After each rainfall, first according to the measured by hourly rainfall, the hydrological model is used to predict the total inflow of Dongzhimen gate and Longtan gate, and the peak flow and its time appears; then, and TS are predicted by the above statistical model. Due to the inability to accurately predict the rainfall process in real-time dispatch, the, and TS can only be amended on a time-by-hour basis as the rainfall progresses. Type 2 operating rules are mainly used as the upper bound for the period-by-period decision.

## 5. Conclusion

Water is the source of life, the blood of industry, the lifeblood of cities and the rational management of water resources are the preconditions for the sustainable development of urban health. How to make disasters into available water resources is an important part of research on water resources utilization management in the new situation. In view of the actual situation of rainstorm in our country, a multi-objective optimization algorithm for city rainwater landscape design optimization is proposed, and the approaches and methods of urban rainwater landscape design are explored. The research shows that the multi-objective is divided into two categories, which are more reasonable and suitable for medium and long-term control and sub-flood scheduling respectively. The proposed multi-objective optimization algorithm can not only reduce the flood but also save the tail of the flood in time. After the example test, the algorithm has the advantages of high accuracy, strong simulation and adaptability, moderate amount of calculation and can meet the general multi-objective optimization analysis needs. This algorithm has strong versatility and provides the future development direction for the urban rainwater landscape design optimization.

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